# Soft Matter



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# PAPER



Cite this: Soft Matter, 2015, 11, 102

Received 19th September 2014 Accepted 14th October 2014

DOI: 10.1039/c4sm02106a

www.rsc.org/softmatter

# 1. Introduction

Patterns arising in soft materials such as elastomers, gels and biological tissues have been receiving growing attention.<sup>1</sup> The understanding and control of the underlying instabilities are crucial for technological applications (microelectronics, microfluidics), for biological systems (wrinkling of human skin or drying fruit<sup>2</sup>) and for medical applications where gels are used as biological scaffolds for tissues or organs. In addition, various patterns which affect the surface of films have been reported in the literature. One of the most studied patterns concerns wrinkles observed when a hard skin, sitting on a soft layer, is compressed. Beyond a critical strain, it results in a periodic sinusoidal deformation of the interface<sup>3-6</sup> for which the periodicity has been derived theoretically.<sup>2,7</sup> When the strain is further increased, a secondary instability occurs leading to a wrinkle-to-fold transition;<sup>8,9</sup> this results in a localization of the deformation.<sup>10</sup> Under a biaxial compressive stress, it has been shown that a repetitive wrinkle-to-fold transition produces a hierarchical network of folds.<sup>11,12</sup> These patterns are observed in various systems such as glassy polymers,<sup>3,13</sup> polyethylene sheets<sup>2</sup> or foams.14 Another group of patterns arises in soft layers supported by rigid substrates.1 Under compressive stresses, an instability often called creasing is manifested by localized and sharp structures at the free surface. These are commonly observed in elastomers,15,16 and hydrogels,17 or in the situation of a rising dough in a bowl.<sup>18</sup> Despite similarities in their morphologies, origins of folds and creases are strongly different. Whereas folds are a secondary instability of wrinkles, creases are a direct deformation of a flat film (creases are also known as sulci19,20). Moreover drying films can produce

# Surface patterns in drying films of silica colloidal dispersions

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We report an experimental study on the drying of silica colloidal dispersions. Here we focus on surface instability occurring in a drying paste phase before crack formation which affects the final film quality. Observations at macroscopic and microscopic scales reveal the occurrence of instability, and the morphology of the film surface. Furthermore, we show that the addition of adsorbing polymers on silica particles can be used to suppress the instability under particular conditions of molecular weight and concentration. We relate this suppression to the increase of the paste elastic modulus.

characteristic crack patterns as they are dried<sup>21,22</sup>. The dryinginduced cracks can invade the surface and propagate simultaneously into the volume of the medium with evaporation of the solvent, resulting in the division of the plane into polygonal domains.

In this paper, we experimentally investigate patterns displayed at the surface of drying films of silica nanoparticles in an aqueous solvent. We discuss the occurrence of these patterns, and we examine their main features using different imaging techniques and rheological measurements. Moreover, the polymer/silica interaction is usually used to tune the mechanical properties of composite films. Consequently, we propose here a method to suppress these structures by adding adsorbing polymers to the silica nanoparticles.

## 2. Experimental

#### 2.1. Controlled drying conditions

Experiments consist in drying a colloidal suspension in a circular glass Petri dish (inner diameter 2R = 5.6 cm) placed in a chamber which has controlled temperature ( $22 \pm 2 \, ^{\circ}$ C) and relative humidity ( $R_{\rm H} = 50 \pm 2\%$ ).<sup>23</sup> The setup is sketched in Fig. 1. The top and bottom walls of the chamber are transparent for visualization by transmitted light. The bottom wall is carefully adjusted horizontally prior to each experiment. Since the sample contrast is very low, the Schlieren technique<sup>24</sup> is used: a honeycomb grid is positioned between the bottom wall and an extended light source. A camera (Nikon D300), located at the top of the chamber, records a photograph each minute.

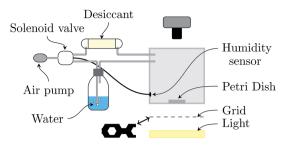
In the following,  $m_i$  varies in the range 1 to 9 g, resulting in an initial thickness  $h_i$  varying in the range from  $\approx 0.3$  to 2.5 mm.

#### 2.2. Colloidal dispersions

We used three aqueous dispersions of silica colloidal particles: Ludox SM-30, HS-40 and TM-50, commercially available from Sigma-Aldrich. The pH is in the range of 9–10, and so the

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**Fig. 1** Experimental setup. Dry or moist air is produced by an air flow from the ambient atmosphere through a desiccant or water respectively to the box. Depending on the humidity measured by the humidity sensor inside the box, a solenoid valve is actioned to converge the humidity to the desired value. A honeycomb grid (represented in its actual size) is used to improve the contrast of the surface corrugations (Schlieren technique).

particle surface bears a high negative charge density.<sup>26</sup> SM-30 is used without treatment, while HS-40 and TM-50 are diluted using pure water (MilliQ quality, resistivity: 18 M $\Omega$  cm) at pH 9.5 by addition of NaOH. A weight ratio of 90/10 (HS-40/water) and 75/25 (TM-50/water) are chosen to obtain similar initial volume fractions. In the following, SM (unmodified), HS and TM designate these dispersions; their main properties are reported in Table 1.

The effect of polymer chains on TM particles is investigated using polyethylene oxide (PEO) or alternatively polyvinylpyrrolidone (PVP). Indeed, a high affinity for silica surfaces is known for PEO and PVP resulting in adsorption on silica particles. To simplify the notations, polymers are denoted as  $P_i$ . Different molecular weights are studied ( $P_i$ : 300 Da,  $P_1$ : 600 Da,  $P_2$ : 3350 Da,  $P_3$ : 6000 Da,  $P_4$ : 35 kDa,  $P_5$ : 600 kDa and  $P_6$ : 8 mDa) for PEO and  $P_7$ : 40 kDa for PVP. Polymers were purchased from Sigma-Aldrich and were dissolved in pure water at pH 9.5. This solution, with a weight concentration of polymers denoted as  $C_p$ is used for the dilution of TM-50. As a result, the final polymer concentration in the TM dispersion is  $C_p/4$ .

The adsorption of polymers on silica particles has been largely studied in the literature.<sup>27–30</sup> In particular, it has been shown, from adsorption isotherms, that silica particles are totally covered with polymers for concentrations above 1 mg m<sup>-2</sup> for PEO<sup>27</sup> and PVP.<sup>31</sup> In our experiments, the polymer concentrations do not exceed  $\leq 0.01$  mg m<sup>-2</sup>, which is much lower than the covering concentration. In this concentration range, polymers adsorb on particles to form necklaces;<sup>29</sup> the dispersed state is stable since the interactions between necklaces are repulsive.<sup>32</sup>

**Table 1** Main properties of silica dispersions used in this paper. The volume fraction is  $\phi_0$ . The values of the particle diameters come from ref. 25 (p. 324)

Silica	Diameter 2 <i>a</i> (nm)	$\phi_0$	$ ho  (\mathrm{kg} \ \mathrm{m}^{-3})$	рН
SM	10	0.15	1180	9.9
HS	16	0.19	1250	9.8
ТМ	26	0.20	1260	9.2

#### 2.3. Visualisation techniques

Observations are done at a macroscopic scale with an optical transmission microscope (DM2500 Leica).

At a microscopic scale, the surface profile is investigated using an Atomic Force Microscope (AFM, Vicco) in tapping mode on dried TM samples (scanning area is  $80 \times 80 \ \mu\text{m}^2$ ) prepared with an initial weight  $m_i = 6$  g. To complete these measurements at the onset of the propagation, an optical profiler is used (Taylor Hobson,  $10\times$ , working distance 7 mm). This contact-less method allows us to measure the surface profile of consolidating materials with a typical surface area of  $1.6 \times 1.6 \ \text{mm}^2$ .

### 3. Results

#### 3.1. Macroscopic observations

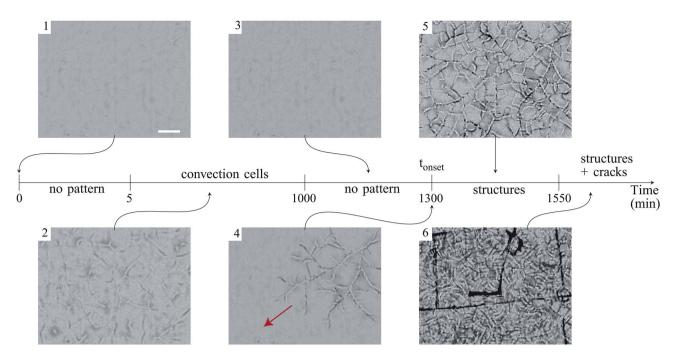
**3.1.1. Temporal evolution.** During water removal, the particles concentrate and the film thickness decreases. At a given time, a network of fine dark lines progressively invades the flat region of the film from the center to the edges. The time evolution of the film surface is shown in Fig. 2. Starting from a homogeneous surface (image 1 in Fig. 2), surface corrugation can be observed after a few minutes of evaporation (image 2 in Fig. 2). The corrugation patterns probably result from Rayleigh-Bénard or Bénard-Marangoni convective instabilities<sup>33</sup>. However, the convective cells disappear after a period of time; the surface recovers its visual homogeneity (image 3 in Fig. 2). Then, at time  $t_{onset}$ , structures progressively invade the surface of the flat film (image 4 in Fig. 2) and result in the pattern shown in image 5 in Fig. 2. Finally, the classical crack pattern forms in the film (image 6 in Fig. 2).

**3.1.2. Onset time.** Starting from a homogeneous surface, the structures appear where the film is thinner, *i.e.* in the center, far from the meniscus. For TM dispersions, we observed that below a critical initial weight  $m_i^c = 1.4 \pm 0.3$  g, *i.e.*,  $h_i^c = 0.4 \pm 0.1$  mm, no structure forms even if cracks do.

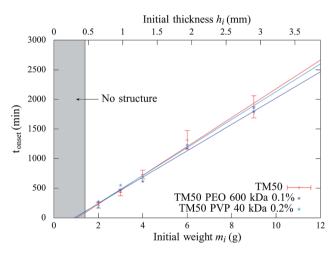
In addition, above this critical initial weight, the onset time  $t_{\text{onset}}$  needed to observe the structure growth, is measured for dispersions of different initial weights deposited in the container, ranging from 1 to 9 g. The results are reported in Fig. 3 and show that the onset time increases linearly with the initial weight.

Similar experiments have been carried out with other samples and the results are summarized in Table 2. For SM and HS samples, no structure appears at the film surface, independent of the investigated range of film thicknesses.

Consequently, we studied the addition of adsorbing polymers only on TM samples. For a sample of initial weight  $m_i = 3$  g deposited in the container ( $h_i = 1$  mm), using PEO with molecular weights larger than 6 kDa, the formation of the structures is suppressed above a critical concentration  $C_p^c = 0.13\%$  (within an uncertainty of 0.03% for  $P_3$  and 0.01% for  $P_4$ ,  $P_5$  and  $P_6$ ). Thus, the weight amount of polymers necessary to suppress the structures is found to be independent of the molecular weight (for  $M_w \ge 6$  kDa). However, for shorter



**Fig. 2** Time evolution of a flat film of a TM sample (initial weight is  $m_i = 6$  g). Each image is focused on the film surface (in the center, far from the Petri dish edge) and is taken at the same region of the film. The arrow in image (4) gives the mean direction of propagation of the structures. Image (6) shows the final pattern made of sinuous structures superposed to a network of channeling cracks. Scale bar: 2 mm.



**Fig. 3** Onset time  $t_{onset}$  of structures as a function of the initial weight and corresponding initial film thickness, for three samples: TM, TM +  $P_5$  (PEO, 600 kDa) at  $C_p = 0.1\%$  and TM +  $P_6$  (PVP, 40 kDa) at  $C_p = 0.2\%$ . The lines are a guide to the eye. The error bars reported for TM samples are similar for other samples.

polymer chains ( $M_w$  < 6 kDa), and for concentrations up to  $C_p = 0.6\%$ , the structures still form.

Moreover, addition of PVP (40 kDa) to TM particles results in suppression of the structures for  $C_p^c(\text{PVP}) = 0.33 \pm 0.03\%$ . We notice that the molecular weight of a polymer unit for PEO  $M_w^{\text{PEO}} = 44 \text{ g mol}^{-1}$  and for PVP  $M_w^{\text{PVP}} = 111 \text{ g mol}^{-1}$ :

$$\frac{M_{\rm w}^{\rm PEO}}{M_{\rm w}^{\rm PVP}} \simeq \frac{C_{\rm p}^{\rm c}({\rm PVP})}{C_{\rm p}^{\rm c}({\rm PEO})} \tag{1}$$

As a result, the structures are suppressed for a critical number of polymer units (160  $\pm$  10 units per colloidal particle, *i.e.* 7.6  $\pm$  0.6  $\mu g~m^{-2}$ ). We checked that the drying kinetics are not affected by the addition of polymers by weight measurements.<sup>23</sup>

**3.1.3. State of the material.** The drying of a colloidal dispersion is a balance between two opposite fluxes: (a) the solvent flux tends to accumulate the particles to the free surface, whereas (b) the diffusion process smooths concentration gradients. The competition between both processes usually states either the formation of a skin at the surface of a drying film or the consolidation in the bulk phase. In that way, the

Table 2         Final state of sample surfaces for the different sample	S
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				$TM + (P_0, P_1, P_2, P_3)$	$TM + (P_4, P_5, P_6, P_7)$	
Sample	SM	HS	ТМ	$\forall C_p$	$C_{\rm p} < C_{\rm p}^{\rm c}$	$C_{\rm p} > C_{\rm p}^{\rm c}$
Observation	∀ <i>h</i> , no pattern	∀ <i>h</i> , no pattern	Patterns if $h > h_c$	Patterns if $h > h_c$	Patterns if $h > h_c$	$\forall h$ , no pattern

relevant dimensionless number is a Péclet number defined as the ratio of a diffusion timescale  $h^2/D$  and an advection timescale  $h^2/V_e$ : Pe $(h) = \frac{V_e h}{D}$ ,<sup>34</sup> where *h* is the film thickness,  $V_e$  is the evaporation rate and *D* is the diffusion coefficient. The evaporation rate is found to be equal to  $V_e \simeq 1 \times 10^{-8} \text{ m s}^{-1}$  under the same drying conditions.<sup>23</sup> The diffusion coefficient is deduced from the Stokes–Einstein relationship  $D = k_{\rm B}T/(6\pi\eta_{\rm s}a)$ , where  $\eta_{\rm s} = 1$  mPa s is the solvent viscosity. From thicknesses lying in the range [0.4, 2.9] mm, the Péclet number is between 0.2 and 1.8. The value close to 1 does not allow us to distinguish between skin formation or consolidation in the bulk.

However, to determine the state of the material, we gently collected a fraction of the material located at the surface of our samples (*e.g.* TM sample,  $m_i = 9$  g, typically 1/4th of the paste thickness); the sample was operated during the propagation of structures and before the apparition of cracks. We measured a volume fraction of  $\phi = 38 \pm 2\%$  which is compatible with an elastic material ( $\phi > 0.35$ ) of non-aggregated particles ( $\phi < 0.61$ );<sup>35</sup> this material, deposited in a test tube filled thereafter with deionized water, can be redispersed after shaking.

#### 3.2. Visualisation

**3.2.1. Optical microscopy.** The propagation of structures was first observed by optical microscopy. The sequence of images in Fig. 4(a, b and c) reveals the dynamics of formation of the structures in the center of the sample. A propagating branch (2) approaches a prior one (1), then crosses. Moreover, in Fig. 4(c), the final pattern in the sequence shows an increase of the structure contrast, and the formation of a new generation of branches and dividing domains. The series of photographs in Fig. 4(d) show a typical detailed process of the splitting of one branch into two branches.

As shown in previous pictures, the structures exhibit an isotropic pattern in the center of the sample. However, while structures propagate in a thickness gradient naturally imposed by the meniscus at the edge of the container, they become preferentially oriented radially and ortho-radially (Fig. 5(b)).

A meniscus at the edge of the container extends over few times the capillary length scale  $\kappa^{-1} = \sqrt{\frac{\gamma}{\rho g}} \approx 2 \text{ mm} (\gamma \text{ is the surface tension of water})$ . At the final stage, we obtain isotropic patterns (Fig. 5(a)) in a region covering 40% of the total surface area which corresponds to the flat film area.

**3.2.2. AFM profilometry.** The surface topography of a TM sample is reported in Fig. 6(a). The typical structure height ranges between 1  $\mu$ m and 4  $\mu$ m. In particular, we notice the asymmetric shape of the surface profile, as an evidence of two inclined planar surfaces connected by a transition region of about 10  $\mu$ m. As a result, such measurements during the propagation of structures are shown in Fig. 6(b). The red region of the surface corresponds to a thicker layer; this can be related to the presence of the microscope objective limiting the evaporation flux.<sup>36</sup> In front of the structures, the film is flat, and an arch-shaped profile is shown at the onset of the instability. During the drying process, this shape evolves to an asymmetric

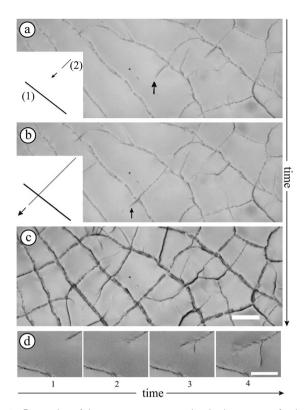


Fig. 4 Dynamics of the structure propagation in the center of a drying TM film. The time laps between pictures (a) and (b) is 21 seconds. The situation indicated by arrows is detailed in the insets. Picture (c) shows the final pattern. (d) The series of photographs show a morphogenetic sequence (time laps between each picture: 1 s) leading to a developed branching process. The scale bars represent 200  $\mu$ m.

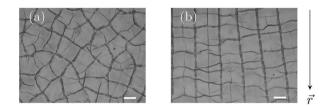
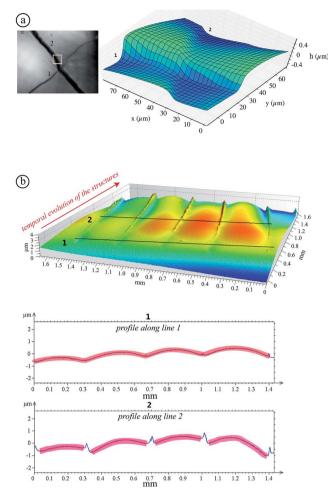


Fig. 5 Final pattern (a) in the center of the Petri dish and (b) at 1 cm from the edge located at the bottom of the picture (The vector  $\vec{r}$  designates the radial direction.). The scale bars represent 100  $\mu$ m.

shape. The kinks present near the junction of arches (bottom graph) are due to the absence of interference fringes with the optical profiler at the singularities resulting in an artifact. Thus, we only consider parts of the profile highlighted in red.

Moreover, in the case of experiments carried out with SM and HS samples for  $m_i \in [2, 12]$  g, no structure can be observed. This statement is also confirmed using AFM, and optical profiler images.

Finally, measurements using AFM and optical profiler techniques reveal the absence of structures in TM with polymers above  $C_p^c$  as in the case of observations using optical microscopy. Note that polymer addition below  $C_p^c$  leads to a lower



**Fig. 6** (a) Surface profile (AFM) of a dried TM sample ( $m_i = 6$  g). The 3D profile on the right corresponds to the region inside the yellow square in the image on the left. (b) Surface profile obtained using an optical profiler: a drying region with propagating structures from the background to the foreground are shown in the profiles along the lines 1 and 2.

structure height. For instance, addition of PEO (600 kDa,  $C_{\rm p} = 0.1\%$ ) decreases the maximum height to 1 µm ( $m_{\rm i} = 6$  g).

#### 3.3. Rheology

In the following the rheological properties of pastes are investigated at the onset of structure formation. In order to compare the elastic moduli of different silica pastes, measurements are performed at a well-defined consolidation time: the onset time for TM films and the same consolidation time for other systems. Samples are prepared using the same protocol: the initial weights range from 7 to 9 g. We collect surface samples corresponding to 4/5th of the film thickness in the center of the container. A part is used for a dried extract in order to deduce the volume fraction  $\phi$ . The paste elastic modulus is measured using a rheometer (Anton Paar MCR501) in the plate-plate geometry (diameter: 24.93 mm) with a solvent trap. The gap is adjusted between 0.3 and 0.7 mm according to the amount of paste used for the measurement. Small oscillatory shear flow tests are performed with an amplitude of 0.2%, and a frequency sweep from 100 Hz to 1 Hz for 200 s per point. Under these conditions, the elastic modulus  $G'(\omega)$  does not vary significantly with the frequency (relative variations lower than 10%) and the deformation amplitude up to a few percent above which the elastic modulus decreases. The average value is denoted by  $G_0$ in the following.

In this way, five samples are considered: SM, HS and TM dispersions and binary mixtures of TM and PEO (600 kDa) at  $C_{\rm p} = 0.2\%$  and  $C_{\rm p} = 0.4\%$ . For TM samples (without polymers), since structures appear at  $\phi = 38 \pm 2\%$ , we selected other samples (where no structures are developed) with a similar volume fraction. The results are shown in Fig. 7. Our results on the HS sample are consistent with values available in the literature.<sup>37</sup> Note that, for all studied samples, the loss modulus ( $G''(\omega)$ ) appears to be at least one order of magnitude lower than  $G_0$ . For pure dispersions, the elastic modulus decreases nearly one order of magnitude when the mean particle size varies from 10 to 26 nm. In contrast, the addition of a small amount of PEO adsorbing on TM particles results in the increase of the paste elastic modulus.

### 4. Discussion

Our observations concerning the dynamics of formation and the characteristics of the pattern show that the structures observed here can be scarcely related to wrinkles. Indeed, wrinkles are periodic deformations of the interface<sup>5</sup> whereas our patterns are clearly localized.

Folds, described as a secondary instability arising from wrinkles,<sup>8</sup> present strong similarities such as the localization of the deformation and the subdivision of domains and crossing patterns.<sup>11</sup> However, the observation of wrinkles is expected but it has never been observed in our systems. Moreover, wrinkles and folds result from the deformation of skin in contact with a

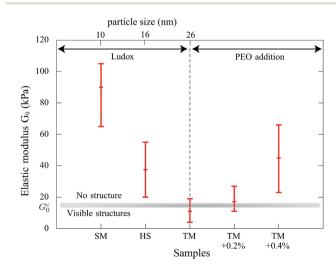


Fig. 7 Rheological measurements of the elastic modulus  $G_0$  obtained from small oscillatory shear flow tests (plate-plate geometry) for different samples of pure particles (SM, HS and TM) and with addition of PEO (600 kDa) in TM. The error bars indicate extreme values.

softer material whereas at the onset of the structure formation, the film seems to behave like a homogeneous paste phase.

Observations at the onset of patterning (top graph of Fig. 6(b)) suggest some morphological similarities with crease patterns of swelling elastomers reported in the literature<sup>16</sup> while the mechanism is different. The observed arches evolve to a "saw-tooth roof shape" as shown by AFM measurements (Fig. 6(a)). This transition is illustrated in the bottom graph of Fig. 6(b) where the onset of the lost of symmetry can be seen. Indeed, this transition may be attributed to the fact that colloidal pastes are able to change their microstructures. A possible explanation of the symmetry breakage from the onset of the instability to the final state can be that any further strain energy is dissipated in the shear of the material (creep flow).

The second question addressed in this paper concerns the absence of structures for SM and HS particles, as well as the suppression by the addition of adsorbing polymers.

The mechanical properties of pastes depend on the colloidal dispersion or the concentration of additional polymers. The strain in the paste phase at the onset time can deduce the elastic modulus. Indeed, assuming that the internal stress during the drying process comes from the flux of water through the porous matrix made by silica particles, the greatest stress occurs at the drying surface where the pore pressure is larger.<sup>38</sup> There, the stress  $\sigma$  scales as follows:

$$\sigma \sim \frac{h\eta_{\rm s}}{3k} V_{\rm e} \tag{2}$$

where *k* is the permeability of the porous material. This expression justifies that below a critical thickness  $h_i^c$ , no structure is visible because the tensile stress is not large enough to trigger the mechanical instability. Estimating the permeability from the Carman-Kozeny relationship at  $\phi = 38\%$  ( $k = 6 \times 10^{-18} \text{ m}^2$ ), we deduce a critical strain  $\varepsilon_c$  at the onset of structure formation:

$$\varepsilon_{\rm c} \sim \frac{h_{\rm i}^{\rm c} \eta_{\rm s}}{3kG_0} V_{\rm e} \simeq 0.2 \tag{3}$$

where  $G_0 = 11$  kPa for TM. It is noteworthy that for this deformation, the elastic modulus of the material is still comparable to the one measured at low deformation amplitudes. Moreover, the elastic modulus is measured just prior to the propagation of the structures (that occurs over a timescale of 10 min) at a controlled volume fraction. Thus, this elastic modulus must be considered as an order of magnitude that could be underestimated, which means that this critical strain could be overestimated.

Measurements show that above a critical elastic modulus, structures are suppressed. This critical value is estimated by  $G_0^c = 15 \pm 5$  kPa from Fig. 7. Indeed, for pastes exhibiting larger elastic moduli, shrinkage induced by the drying is withstood by the paste network leading to a low strain. Further shrinkage is frustrated by adhesion of the paste onto the substrate and results in tensile stress and crack formation. However, for pastes exhibiting lower elastic moduli, the strain is larger leading to possible surface corrugations. eqn (3) also suggest that  $G_0^c$  should depend on the film thickness if  $\varepsilon_c$  does

not. From our observations, we cannot conclude on a dependence of  $G_0^c$  with the film thickness because near the threshold, the presence or absence of structures is difficult to be stated. Indeed, the structure density decreases with the film thickness as shown in the inset of Fig. 3.

In the case of pure colloidal dispersions (SM, HS, and TM), the particle size affects the elastic modulus (Fig. 7), consequently the permeability. Indeed, fitting the elastic moduli as a function of the particle size with a power law,  $G_0 \propto a^p$ , leads to values  $p \in [-1, -3]$ . The inaccuracy comes from the large error bars and the little number of available samples. Taking into account the particle size dependency in the permeability with the Carman-Kozeny model, the deformation varies as  $\varepsilon \propto$  $a^{-(p+2)}$ . A power coefficient *p* lower than -2 would be consistent with our observations on the suppression effect. We can also note that our description assumes that changing Ludox only results in varying particle size. It is worth noting that other parameters may have effects, such as polydispersity (see ref. 25 measurements) which can modify the (p. 324) for permeability.39

Finally, we also observed that patterns are hierarchical (Fig. 2) which introduces different lengthscales. The final pattern settles after 250 minutes in the given example. This suggests that the refinement is related to the consolidation of the material that can be analyzed by the increase of the elastic modulus in time which increases the stress in the material.

# 5. Conclusion

In this paper, we report experimental observations on surface instabilities during the drying of silica colloidal dispersions. These patterns grow if films are thicker than a critical thickness and that the onset time increases linearly with the initial film thickness and is concomitant with a paste phase sitting on the substrate. Measurements using microscopy techniques highlight the surface corrugations resulting first in arches that evolves to a saw tooth roof shape. We also provide a method to prevent these patterns by the addition of a small amount of polymers which increases the material elastic modulus. From this technique, we estimated a critical elastic modulus for structure formation.

As a perspective, it would be interesting to refine the description of the evolution from arches to the saw-tooth roof shape which is attributed to a creep flow caused by the nature of the material. Thus, a competition between the creasing instability and the creep flow may exist in the selection of the final characteristic distance separating structures. In particular, in a future study, the evolution of structures could be related to the characteristics (onset time and final size) of the different generations in order to establish a criterion for the distance between structures and to precise the influence of loss of symmetry on the development of instability. Further theoretical developments might focus on similarities and differences of surface instabilities in visco-elastic-plastic materials compared to visco-elastic gels.

# Acknowledgements

The authors thank the Triangle de la Physique for the rheometer (Anton Paar, MCR 501) and A. Aubertin for designing the experimental setup. We are grateful to B. Cabane, J.-P. Hulin, G. Gauthier and C. Quilliet for fruitful discussions and A. Chennevière, C. Poulard and F. Restagno for guidance and for sharing their AFM and optical profiler.

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